

1. (a) If my parents do not ask me to do my chores, then I don't mind doing them.
- (b) If I mind doing my chores then my parents ask(ed) me to do them.
- (c) If I don't mind doing my chores, then my parents have not asked me to do them.

2.

$$\begin{aligned}
 \neg(p \wedge (\neg p \vee q)) &\equiv \neg p \vee \neg(\neg p \vee q) \\
 &\equiv \neg p \vee (p \wedge \neg q) \\
 &\equiv (\neg p \vee p) \wedge (\neg p \vee \neg q) \\
 &\equiv T \wedge (\neg p \vee \neg q) \\
 &\equiv \neg p \vee \neg q
 \end{aligned}$$

p	q	$p \leftrightarrow q$	$p \rightarrow q$	$q \rightarrow p$	$(p \rightarrow q) \wedge (q \rightarrow p)$
F	F	T	T	T	T
F	T	F	T	F	F
T	F	F	F	T	F
T	T	T	T	T	T

Note the third column and final column match, establishing logical equivalence.

4. (d) $\{\{\}, \{0\}, \{1\}, \{0, 1\}\}$
 - (e) $\{-2, -1, 2\}$
 - (f) \emptyset
 - (g) Since $A \times A \times B$ has coordinate triples (a_1, a_2, b) , and there are 5 possible values for both a_1, a_2 but only two for b , that means there are $(5)(5)(2) = 50$ elements.
 - (h) Since A has 5 elements, the subsets of A correspond to the 5-bit binary words, 00000, 00001, 00010, ..., 11111, of which there are $2^5 = 32$.
 - (i) The only values a characteristic function produce are 0 and 1, so the range is $\{0, 1\}$.
 - (j) The inputs from \mathbb{R} that would result in the output 1 are precisely those x -values in the interval $(-3, 3]$.
 - (k) $f(A) = \{f(-2), f(-1), f(0), f(1), f(2)\} = \{-1, -1, 0, 0, 1\} = \{-1, 0, 1\}$
 - (l) $f^{-1}(B) = \{x \in A \mid (f(x) = 0) \vee (f(x) = 1)\} = \{0, 1, 2\}$
5. (a) S (b) B (c) N
6. (a) $\exists x \forall p V(x, p)$ has negation $\neg \exists x \forall p V(x, p) \equiv \forall x \exists p (\neg V(x, p))$, which leads to this:
"Given anyone in the class, there is some national park that person has not visited."
 - (b) "There is no path from here to there, or there are at least two paths from here to there."
 - (c) We have the equivalence $(p \rightarrow q) \equiv (q \vee \neg p)$, and that has negation $\neg(q \vee \neg p) \equiv \neg q \wedge p$.
Translating back to English, this is "I fall asleep and my roommate is snoring."