

Stat 145, Mon 25-Oct-2021 -- Mon 25-Oct-2021
Biostatistics
Spring 2021

Monday, October 25th 2021

Due)) PS10 due at 11 pm

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Wk 9, Mo

Topic:: Student t distributions

Read:: Lock5 6.4-6.6, 6.13

HW:: WW ch06Part1 due Thurs.

Test 2: Fri. Nov. 5

Why t-distributions?

- arise in context of quantitative data. Why?
- no need when doing one-proportion (nor two-proportion) inference
- for 1-sample mean settings, $df = n-1$, $n = \text{sample size}$

Practice with

1. summarized data

n=27 healthy white males, mean systolic bp: 114.9 with s=9.3

- (a) Give a 92% CI for true mean bp among healthy white males
- (b) Test $\mu = 118$ vs. a 2-sided alternative

2. raw data

dogs, from boot package: use lvp variable (left ventricular pressure)

BodyTemp50, from Lock5withR package

t.test() command

have raw data

3. paired data

hypotheses

Wetsuits data

Ex. 1)

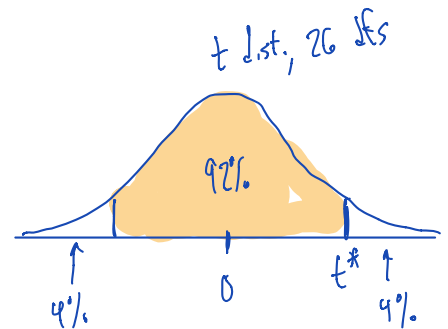
$$\bar{x} = 114.9, \quad s = 9.3$$

$$t^* = qt(0.96, df = 26) = 1.822$$

(a)

$$\text{point est} \pm (\text{critical value}) (SE_{\bar{x}})$$

$$114.9 \pm (1.822) \frac{9.3}{\sqrt{27}}$$



(b) $H_0: \mu = 118$ (null value) vs. $H_a: \mu \neq 118$

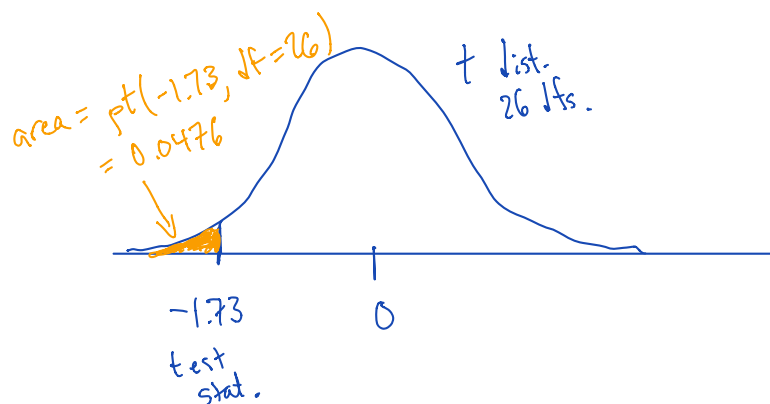
Still have $\bar{x} = 114.9$

est. $SE_{\bar{x}} = \frac{9.3}{\sqrt{27}}$

Standardized score (test statistic)

$$t = \frac{\bar{x} - \mu_0}{SE_{\bar{x}}} = \frac{114.9 - 118}{9.3/\sqrt{27}} = -1.732$$

Guiding principle for conducting t-hypothesis tests: must standardize your point est.



$$P\text{-value} = 2(0.0476) = 0.0952$$

Ex.) BodyTemp50 - BodyTemp variable

fairstats says $\bar{x} = 98.26$, $s = 0.7653$

Now we could do a CI (like part (a) of last example)

If a 98% CI

$$SE_{\bar{x}} = 0.7653 / \sqrt{50}$$

$$t^* = qt(0.99, df=49)$$

$$\bar{x} \pm (t^*)(SE_{\bar{x}})$$

Or, we could do hyp. test

$$H_0: \mu = 98.6 \quad \text{vs.} \quad H_a: \mu \neq 98.6$$

$$\text{test statistic} \quad t = \frac{\bar{x} - 98.6}{SE_{\bar{x}}}$$

Convenient command in RStats for doing all this: `t.test()`

but you have to have raw data to use it.

(So, can't use it on Example 1.)

> `t.test(~ BodyTemp, data = BodyTemp50)`

or, for our needs

> `t.test(~ BodyTemp, data = BodyTemp50, mu = 98.6, conf.level = 0.98)`

Ex.) Paired data

data set: Wetsuits

$$H_0: \mu_{\text{Diff}} = 0$$

From every swimmer/case - my interest is

not in wetsuit time

not in nowetsuit time

but in difference: wetsuit - nowetsuit

$n = 12$ here

You can see the 12 differences using

> with (Wetsuits, Wetsuit - NoWetsuit)

You can test H_0 vs. $H_a: \mu_{\text{Diff}} \neq 0$ using

> t.test(\sim Wetsuit - NoWetsuit, data = Wetsuits)

indicates you want
the two columns
subtracted